Soft Matter

Advancing liquid contact line on visco-elastic gel substrates: stick-slip *vs.* continuous motions†

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We studied the dynamics of water sessile droplets advancing on hydrophobic and visco-elastic poly(styrene-butadiene-styrene)(SBS)–paraffin gel substrates at various inflation rates. During the advancing process, the droplet contact line exhibits three different regimes of motions. When the contact line advances at a high velocity, it moves continuously with a constant contact angle. As the contact line slows down, it starts a stick-slip motion: the contact line is pinned at a certain position and then suddenly slips forward. With further decrease of the velocity, the contact line stops the stick-slip motion and continuously advances again. The observed threshold values for the transitions of the contact line motions (continuous–stick-slip–continuous) indicate that the rheology of the gel drastically affects the dynamics of liquid on its surface. We suggest that on visco-elastic gels, the moving contact line exhibits both aspects of wetting on elastic solids and wetting on viscous liquids depending on the characteristic frequency of the gel surface deformation. At an intermediate regime, the stick-slip motion of the contact line appears. We also propose a simple geometrical model in the stick-slip regime which allows us to relate the jumps of the droplet radius to the jumps of the apparent contact angle.

I Introduction

Gels, cross-linked network of polymers swollen with solvent, are materials which have been attracting continued interest for decades since they are complex nature of matter[1,2] and they also have promising potentials for applications in food processing, medical science,[3] and organic electronics.[4] One of the important challenges is to understand and to control the interfacial properties of gels, as they determine adhesion and friction[5–7] (*e.g.* cartilage replacement), surface tension and wetting properties[8–11] (*e.g.* soft contact lens, anti-condensation coating, encapsulation in consumer products). Here we focus on the wetting of liquids on gel surfaces.

Wetting dynamics is still an active subject of research even on "hard" solid surfaces because of the need to patch up classical hydrodynamics near the contact line.[12,13] On gels, the situation would be more complex as the wetting liquid can cause a large deformation on the gel surface which successively affects the statics and dynamics of the contact line.[14] The deformation of the gel surface is caused by two mechanisms: by

the balance between the interfacial tensions and elastic resistance of the gel and by the volume exchange between the liquid and gel. Intuitively, the behavior of the contact line on gels might be understood in analogy with the wetting on soft surfaces like an elastomer[15–17] or with the wetting on permeable surfaces like porous media.[18,19] However, as gels have an unusual nature between solids and liquids, the wetting on gels would be even more complex than those situations. Previously, Holmes *et al.*[20] and Kajiya *et al.*[21] studied the spreading behavior of liquid droplets on gels, which are under the swelling equilibrium, and they observed a strong coupling between the volume exchange and contact line dynamics.

In this paper, we are turning our attention to a different aspect of the gel complexity, *i.e.*, the rheology of gels. We studied the dynamics of water sessile droplets being inflated on poly(styrene-butadiene-styrene)(SBS)–paraffin gel substrates. As the SBS–paraffin gel is hydrophobic and there is no volume exchange between the droplet and gel, the possible factor causing the surface deformation is the interfacial tensions applied at the contact line. Nevertheless, unlike the case of wetting on an elastomer, the droplet contact line exhibits quite complex behaviors, *i.e.*, the contact line shows two regimes of continuous advancing motion and a stick-slip motion depending on the inflation rate and droplet radius. The stick-slip motion of the contact line was previously observed by Pu *et al.* during wetting on thin polymer films.[22,23] Here we found that on a SBS–paraffin gel, there are three different regimes of the contact line motion, *i.e.*, continuous, stick-slip, and another

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continuous motion. We discuss how the transitions of these contact line motions are characterized by the parameters such as the frequency of the surface deformation and the gel rheology, and propose a possible mechanism for the present phenomena.

II   Experimental section

Poly(styrene-butadiene-styrene)(SBS)–paraffin gels were used for the gel substrates and distilled water (Milli-Q Integral; Millipore, USA) was used for the liquid.

SBS powders (G1682; Kraton Polymers, USA) were dissolved in paraffin (Norpar15; ExxonMobil, USA) heated in a water bath at 90 °C. After SBS was completely dissolved in paraffin, the solution was poured into a gel mold and was cooled down to ambient temperature. The gel mold consists of two glass plates separated by a rubber spacer. The gel samples were 70 mm in length, 20 mm in width and 3 mm in thickness. Gels of various SBS concentrations were prepared. The mass concentration of SBS c_{SBS} was varied from 8% to 25%. The typical roughness of the gel surface was measured to be of the order of 10 nm by an optical profiler.

The rheological property of the gel was measured by a strain-controlled rheometer (Physica MCR 500; Anton Paar, Austria) with a stainless steel cone and a plate sample cell. The radius of the plate is 50 mm, the cone angle is 1°, and the gap between the cone and plate was set to 0.052 mm. A shear strain amplitude was set to 1%. A strain sweep test for selected samples showed that this was sufficiently small to keep rheological properties in the linear viscoelastic range. The experiments were conducted at 20 ± 0.2 °C and performed at frequencies from 10^{-4} Hz to 10 Hz.

The curves of the storage modulus G' and loss modulus G'' against frequency are plotted in Fig. 1 for the gel of $c_{SBS} = 10\%$, and typical values of the gel properties (G' at $f = 1$ Hz and crossover frequency f_{cross}) are listed in Table 1 for $c_{SBS} = 8, 10, 12, 16\%$. Note that two types of measurements were conducted: one at low frequencies (10^{-4} to 10^{-2} Hz) to determine f_{cross}, and the other at a wide range of frequencies (10^{-4} to 10 Hz) to determine G' at $f = 1$ Hz. For $c_{SBS} = 12\%$ and 16%, f_{cross} was obtained by extrapolating the curves of G' and G''.

Table 1 Typical values of the storage modulus G' at 1 Hz and crossover frequency f_{cross} where $G''/G' = 1$ for the SBS–paraffin gel

c_{SBS} (%)	8	10	12	16
G' (kPa)	2.53	5.72	13.1	19.4
f_{cross} (1 s^{-1})	3.3 ± 10^{-3}	7.2 ± 10^{-4}	5.3 ± 10^{-5}	2.6 ± 10^{-6}

The inflation experiment of a water droplet on the gel was conducted as follows. A water droplet was placed on the gel by a micro-syringe. The syringe was connected to a motor syringe pump (Model 33; Harvard Apparatus, USA), and it supplies water to the droplet and inflate it at a constant volume rate q. The inflation rate q was varied from 1 μl min^{-1} to 200 μl min^{-1}. From the side and top of the droplet, the shape of the droplet was monitored by 2 CCD cameras (Model A101fc and Model PLA1000; Basler, Germany) with magnification lenses (CCTV lens; Pentax, Japan).

Alternatively, for a static contact line, the surface profile of the gel was measured by an optical profiler (Microsurf 3D, Fogal Nanotech, France) with a 5× objective lens. A sessile droplet was placed on a SBS–paraffin gel. Successively, the gel surface profile close to the contact line was measured at different time steps.

III   Experimental results

A   Stick-slip motion of the contact line

Fig. 2(a)–(d) show sequential pictures of a water droplet being inflated on a SBS–paraffin gel of $c_{SBS} = 10\%$ at an inflation rate $q = 20$ μl min^{-1}. During the inflation process, the droplet contact line exhibits a stick-slip motion. The contact line is pinned at a certain position. As the inflation proceeds, the contact angle gradually increases while the contact line stays at the same position. Then suddenly, the contact line slips forward over a certain distance. Successively, the contact line repeats this stick-slip motion.
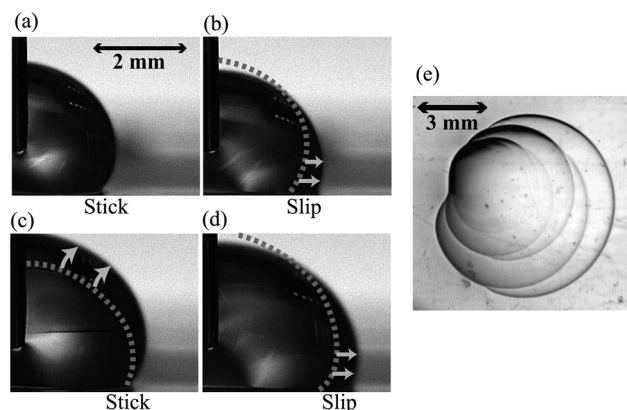
Fig. 2 (a–d) Sequential pictures of water droplet being inflated on a SBS–paraffin gel ($c_{SBS} = 10\%$) at an inflation rate $q = 20$ μl min^{-1}. In images (b–d), a contour line of the previous droplet shape is drawn as a dotted line. During the inflation process, the contact line shows a stick-slip behavior, i.e., the contact is fixed during a certain moment and then quickly advances. (e) A picture of the gel surface taken after the inflation process is finished and the droplet is removed. The droplet leaves multiple circular patterns.
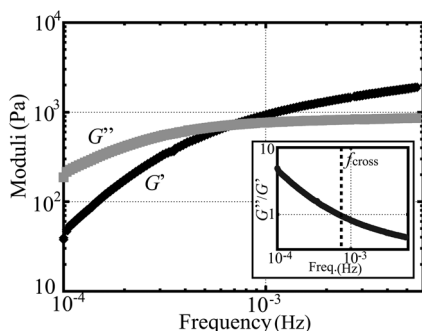

Fig. 1 Storage and loss moduli G' and G'' of the paraffin gel ($c_{SBS} = 10\%$) at 20 °C. Phase angle tan $\delta = G''/G'$ is shown in the inset.

After the inflation process, the water droplet was removed quickly and a picture of the gel surface was taken as it is shown in Fig. 2(e). Multiple circular stripe patterns are observed on the gel surface. These circular patterns indicate that the droplet contact line locally pulls up the gel surface, forming ridges. After a sufficiently long time, i.e., 2–3 h, these ridges totally disappear and the gel surface goes back to completely flat. (Note: by an analogy with the leveling of a thin liquid film,[13] the typical relaxation time of the ridge can be estimated of the order $\eta R^4/\gamma_s H^3$, where η is the gel viscosity, γ_s is the gel surface tension, R is the droplet radius, and H is the average gel thickness. Substituting R, $H = 1$ mm, $\eta = 2 \times 10^5$ Pa s (measured by rheometry at low frequencies), and $\gamma_s = 30$ mN m^{-1}, it is ca. 6000 s, which is close to the relaxation time 2–3 h observed here.)

From the sequential pictures, the radius R and the contact angle θ of the droplet are measured as a function of time and are plotted in Fig. 3. The data on gels of 2 different SBS concentrations are shown: $c_{SBS} = 10\%$ for (a) and (b), $c_{SBS} = 25\%$ for (c) and (d). The inflation rate is fixed at $q = 20$ μl min^{-1}.

The plots in Fig. 3(a) and (b) clearly show that on a gel of $c_{SBS} = 10\%$, the droplet contact line exhibits two different motions. At an early stage of the inflation process ($t < 160$ s) while the droplet radius R is still sufficiently small ($R < 2$ mm), the contact line advances continuously with a nearly constant contact angle $\theta_a \approx 100°$. As R becomes large at a later stage ($t > 160$ s, $R > 2$ mm), the contact line starts the stick-slip motion, i.e., the droplet radius R stays at the same value during a certain moment then suddenly increases. Looking at the contact angle, once the contact line sticks, θ starts to increase from θ_a. As θ reaches a critical value $\theta_b \approx 110°$, the contact line slips forward and θ goes back to the value θ_a.

On the other hand, on a rigid gel of higher polymer concentration $c_{SBS} = 25\%$ (Fig. 3(c) and (d)), the stick-slip motion of the contact line is not observed during the whole inflation process. The droplet contact line always advances continuously with a constant contact angle close to θ_a.

B Dependence on q and R: three regimes of contact line motion

For a quantitative analysis, inflating experiments were conducted at various inflating rates q. Fig. 4 shows the plots of the droplet radius and contact angle against time on gels of $c_{SBS} = 10\%$ at 3 different inflation rates: (a) $q = 200$ μl min^{-1}, (b) 20 μl min^{-1}, and (c) 2 μl min^{-1}. Since the total inflation time varies largely by q, for the comparison of each data, the droplet radius R and time t are normalized by the referential values R_r and t_r. Here R_r is arbitrarily selected as 4 mm, and t_r corresponds the time at which the droplet radius reaches R_r (in our experiment, the typical value of t_r is 70 ± 5 s for $q = 200$ μl min^{-1}, 700 ± 50 s for $q = 20$ μl min^{-1}, and 6000 ± 300 s for $q = 2$ μl min^{-1}).

Depending on the inflating rate q, the droplet contact line remarkably changes its behavior, which also varies the pattern remaining on the gel surface after the inflation process.

● At a high inflation rate ($q = 200$ μl min^{-1}), the contact line advances continuously with a constant contact angle $\theta_a \approx 100°$ during the whole inflation process (Fig. 4(a)). When the droplet is removed after the inflation, the gel surface is flat and no clear trace is observed.

● At an intermediate inflation rate ($q = 20$ μl min^{-1}), the contact line initially exhibits the continuous advancing motion. As the droplet radius reaches a critical value ($R \approx 2.2$ mm), the contact line starts the stick-slip motion (Fig. 4(b)). θ varies between $\theta_a \approx 100°$ and $\theta_b \approx 110°$. After the inflation process, multiple circular ridges remain on the gel surface.

● At a low inflation rate ($q = 2$ μl min^{-1}), the contact line exhibits the stick-slip motion even at a very early stage of the
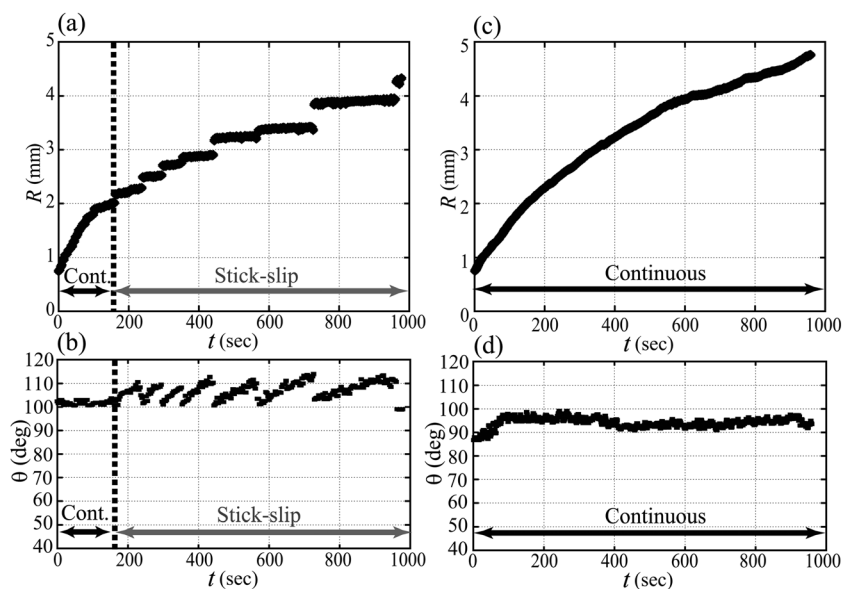

Fig. 3 Plots of the radii and contact angles of droplets against time being inflated on SBS–paraffin gels at an inflation rate $q = 20$ μl min^{-1}. Data on gels of two different SBS concentrations are shown. (a) Radius and (b) contact angle of the droplet on a gel of $c_{SBS} = 10\%$. (c) Radius and (d) contact angle of the droplet on a gel of $c_{SBS} = 25\%$.
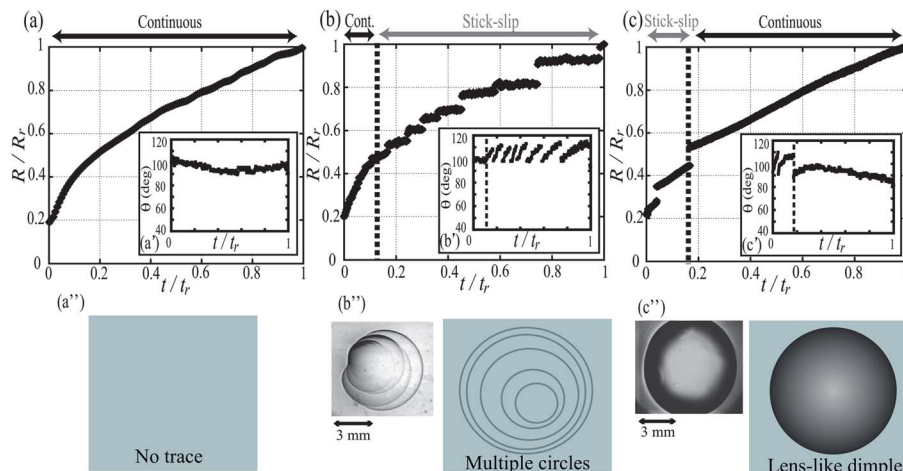
Fig. 4 Plots of the normalized radii of droplets against normalized time being inflated on SBS–paraffin gels of $c_{SBS} = 10\%$ at three different inflation rates. For comparison, the radius is normalized by a referential value $R_r = 4$ mm, and the time is normalized by a time t_r at which the radius reaches R_r. The inflation rates are (a) $q = 200$ μl min^{-1}, (b) $q = 20$ μl min^{-1}, and (c) $q = 2$ μl min^{-1}. The contact angles are also plotted in the insets (a'), (b') and (c'), and the pictures and schematic images of the gel surface after the inflation process are shown in the insets (a''), (b'') and (c'').

inflation process. As the droplet radius increases, now the contact line stops the stick-slip motion and starts to advance continuously again (Fig. 4(c)). At this moment, the contact angle θ also stops oscillating between θ_a and θ_b and keeps almost the same value θ_a. After the inflation process, the droplet leaves a single large lens-like dimple instead of the multiple circular ridges. (Note: rigorously, θ_a is not constant in the continuous motion and it slightly decreases with the increase of the droplet radius. This means that θ_a is not really a contact angle in a quasi-static limit but rather a value of the dynamic contact angle. Nevertheless, as the change of θ is sufficiently small, here we treat θ_a as a constant of the order of $100°$.)

In order to check that the observed contact line behaviors are peculiar on the SBS–paraffin gel substrates, we conducted a supplemental experiment by inflating water droplets on a chemically crosslinked silicone elastomer (Sylgard 184; Dow Corning, USA) of Young's module ≈ 10 kPa. It was observed that on an elastic silicone elastomer, the droplet contact line always advances smoothly with a constant contact angle during

the whole inflation process irrespective of the inflation rate ($q = 2$ μl min^{-1}, 20 μl min^{-1}, 200 μl min^{-1}).

From the multiple measurements of R and θ at various inflation rates q, we explored the motion which the contact line exhibits as a function of R, and plotted them in the diagram shown in Fig. 5. It is clearly seen that depending on q and R, there are three different regimes of the contact line motion.

(i) The smooth advancing regime at high q and small R.

(ii) The stick-slip regime at intermediate q and R.

(iii) The second smooth advancing regime at low q and large R.

C Local deformation of the gel surface at a contact line

To explore the local deformation of the gel surface at the droplet contact line, a sessile droplet of volume 7.5 μl was placed on a SBS–paraffin gel and the surface profile close to the contact line was measured by an optical profiler. Fig. 6(a) shows the surface profiles of two gels ($c_{SBS} = 10\%$ and 16%) measured shortly after the placement of the droplet ($t = 2$ min), and Fig. 6(b) shows the time dependence of the surface profile ($c_{SBS} = 10\%$, $t = 2$, 6, and 10 min).

On both gels, the gel surface is pulled up and a ridge is formed close to the contact line. Since the SBS–paraffin gel is hydrophobic and there is no volume exchange between the droplet and gel, the surface ridge is considered as a consequence of the balance between the vertical component of liquid surface tension and the elastic resistance of the gel in analogy with the problem of liquid droplets on an elastomer.[24–26] This can be confirmed by fitting the profile in Fig. 6(a) with the theoretical curve of the elastic surface ridge due to the capillary force proposed in ref. 24 and 25

$$h(x) \approx \frac{h_0}{2\pi} \ln\left(\frac{d}{x}\right). \tag{1}$$

The fitting parameter h_0 corresponds $\gamma \sin \theta / G$ where G is the shear modulus of the gel, θ is the droplet contact angle, γ is the surface tension of water ≈ 72 mN m^{-1}, and the parameter d

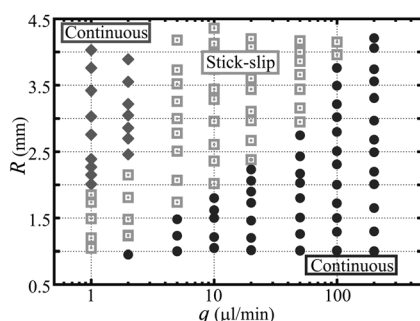**Fig. 5** Diagram of the three different regimes of the contact line motion observed on gels of $c_{SBS} = 10\%$. Data of various droplet radii R and inflation rates q are plotted. The three regimes are distinguished by different symbols, i.e., (i) circle: continuous advancing motion observed at high q and small R, (ii) square: stick-slip motion, and (iii) diamond: continuous advancing motion at low q and large R.
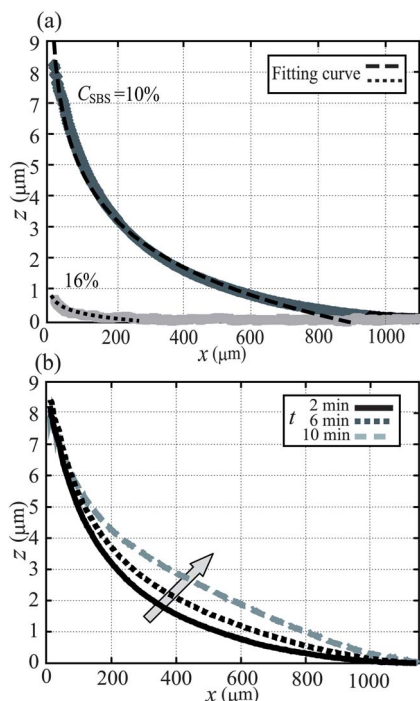
(a)

(b)

Fig. 6 Cross-sections of the gel surface profiles close to the contact line of the water droplet of volume 7.5 µl. The position $x = 0$ indicates the position of the contact line. Note that the profile data were obtained from $x \geq 10$ µm which is our limit of resolution. (a) Gel surface profiles of 2 different c_{SBS} (10%, 16%). The profiles were measured 2 minutes after the placement of the droplet. Bold lines indicate the experimental data, and the dashed lines are the fitting curves of the theoretical formula in ref. 24 and 25. (b) Time evolution of the surface profile on the gel of $c_{SBS} = 10\%$.

indicates the macroscopic cutoff length of the surface ridge. (Note: in this model, $h(x)$, as well as $h'(x)$, diverges at the contact line $x = 0$. More elaborated models have been developed recently[27–29] by introducing a microscopic cut-off length due to the substrate surface tension as we will discuss later in Section IV-C. However, on a scale larger than our resolution ≥ 10 µm, these models also give a similar logarithmic profile. Therefore, we use the model of ref. 24 and 25 for simplicity.)

Both experimental data fit well with the theoretical curves, giving the fitting parameters $h_0 = 14.4$ µm and $d = 840$ µm for $c_{SBS} = 10\%$, and $h_0 = 1.64$ µm and $d = 170$ µm for $c_{SBS} = 16\%$. The typical lengths of h_0 and d are thus sufficiently smaller than the gel thickness. From the obtained value of h_0, the shear moduli of gels G are calculated to be 5.1 kPa for $c_{SBS} = 10\%$ and 42 kPa for $c_{SBS} = 16\%$, which are close to the values measured by rheometry.

Meanwhile, the profile of the surface ridge is not persistent as it is shown in Fig. 6(b). If the contact line stays at the same position on the SBS–paraffin gel, the foot of the surface ridge gradually expands outward and the profile of the ridge becomes less steep.

IV Discussion

In this chapter, we will discuss why the contact line exhibits three different motions (i)–(iii) as seen in Fig. 5, and propose simple geometric considerations in the stick-slip regime (ii).

A Three contact line motions: separation by the characteristic frequency

Considering that both the parameters q and R affect the velocity of the advancing contact line, here we estimate the apparent mean contact line velocity v. v is determined as the velocity of the contact line supposing that the droplet always keeps the contact line advancing continuously with a constant contact angle θ_a at given q and R. (Note that v is not the actual contact line velocity in the stick-slip regime.) From the change of the droplet volume

$$V_{drop} = \frac{\pi R^3}{3}(2 - 3\cos\theta_a), \tag{2}$$

by the constant volume rate q

$$dV_{drop} = qdt, \tag{3}$$

v is calculated as

$$v = \frac{dR}{dt} \approx \frac{q}{2\pi R^2}, \tag{4}$$

as the advancing angle θ_a is close to 90° in our experiment.

In order to compare the contact line behavior with the rheological properties of the gel, we further estimate the characteristic frequency of the gel surface deformation at the moving contact line. Looking back at Fig. 6, the surface deformation is maximum at the contact line and it reaches zero at distances larger than the droplet radius R. Supposing the situation that the droplet is moving forward or backward around a certain point of the gel, the surface on that point rises as the contact line approaches and then falls as the contact line goes away. The typical period of the surface rise and fall τ is thus given by dividing the scale of the surface deformation R by the
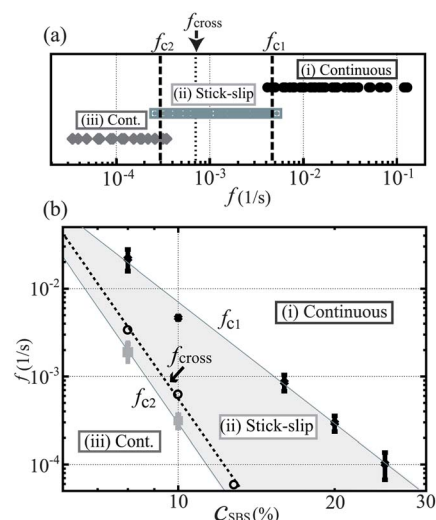

Fig. 7 (a) Replot of the data in Fig. 5 against the characteristic frequency $f = q/2\pi R^3$. The crossover frequency f_{cross} where $G''/G' = 1$ is marked by an arrow. Two critical frequencies f_{c1} and f_{c2} are observed which separate the different regimes. (b) Plot of the two critical frequencies f_{c1} and f_{c2} against SBS concentration of the gel c_{SBS}. The crossover frequencies of gels f_{cross} are plotted as hollow circles for reference.

contact line velocity v. Its inverse is the characteristic frequency of the surface deformation,

$$f = 1/\tau = v/R \qquad (5)$$

From the data points in Fig. 5, we calculated the characteristic frequency and re-plotted the diagram as a function of f in Fig. 7(a). It is clearly observed that the three regimes of the contact line motions (i)–(iii) are separated against f, giving two critical frequencies which characterize the transition between the different regimes: f_{c1} separates between the (i) continuous advancing motion at a high frequency and (ii) stick-slip regime, and f_{c2} separates between the (ii) stick-slip regime and (iii) continuous advancing motion at a low frequency. Comparing this diagram with the rheology of the gel in Fig. 1, it is also seen that the crossover frequency f_{cross} where the two moduli correspond with each other $G''/G' = 1$ is between these two critical frequencies f_{c1} and f_{c2}.

To explore if the critical frequencies f_{c1} and f_{c2} depend on the property of the gel, we conducted the inflation experiments of water droplets on gels of various SBS concentrations. Fig. 7(b) shows a plot of f_{c1} and f_{c2} as a function of c_{SBS}. For reference, the crossover frequency of the gel f_{cross} obtained by rheometry is also plotted. It is observed that both the critical frequencies f_{c1} and f_{c2} decrease with the increase of c_{SBS}, indicating that f_{c1} and f_{c2} have a dependence on f_{cross}. On a rigid gel of high SBS concentration ($c_{SBS} = 25\%$) having a low f_{cross}, the regime (i) becomes prominent in a wide range of f and the value of f_{c1} becomes considerably low ($\approx 10^{-4}$ 1 s^{-1}). In contrast, on a soft gel of low SBS concentration ($c_{SBS} = 8\%$) having a high f_{cross}, both f_{c1} and f_{c2} drastically shifted to higher values ($f_{c1} \approx 2.2 \times 10^{-2}$ 1 s^{-1} and $f_{c2} \approx 2.0 \times 10^{-3}$ 1 s^{-1}), and the contact line mostly takes the regimes (ii) and (iii).

B   Mechanism of the contact line motion transition

Based on the results in the previous sections, we propose a mechanism for the transition between the three contact line behaviors.

As discussed in Section III-C, initially the surface deformation at the contact line is caused by the balance between the surface tension of the liquid and elastic resistance of the gel. However, as the SBS–paraffin gel is visco-elastic, when the contact line stays close to its initial position, the elastic resistance of the gel gradually relaxes and the gel creeps to evolve a surface as shown in Fig. 6(b). After a sufficiently long time, the surface ridge changes its shape to a gradual surface rise like the capillary ridge formed at the contact line of liquid on the surface of another liquid.[30]

Considering the change of the surface deformation due to the visco-elastic nature of the gel,[31,32] the transition of the contact line motions can be understood in terms of the characteristic frequency f of the surface deformation. Fig. 8 illustrates schematically the mechanism of the three contact line motions (i)–(iii).

● Regime (i): when the contact line advances quickly and the characteristic frequency is high ($f \gg f_{cross}$), the gel substrate responds as an elastic solid to the motion of the contact line. In
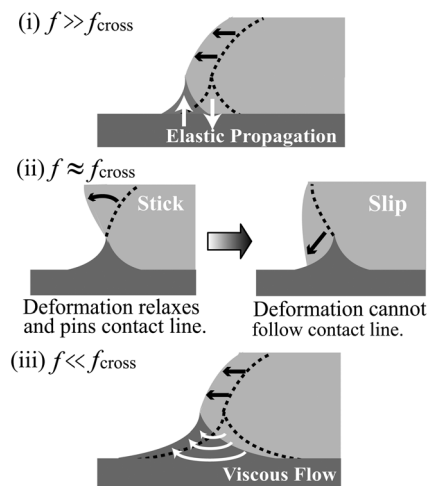

Fig. 8 Behaviors of the contact line and of gel surface deformation at different regimes (i)–(iii).

this situation, the surface deformation at the contact line is an elastic ridge pulled by the surface tension of the liquid. Therefore, the elastic ridge can always follow the motion of the contact line at which the force is locally applied, resulting in the continuous advancing motion (in the SBS–paraffin gel, the elastic deformation can propagate up to a velocity of the elastic wave $\sqrt{G/\rho} \sim 1$ m s^{-1},[33] which is much higher than the velocity in our experiment).

● Regime (ii): as the velocity of the contact line decreases and f comes close to the crossover frequency ($f \approx f_{cross}$), now the response of the gel surface is not purely elastic. Until the contact line advances over a distance proportional to R, the elastic resistance of the gel already starts to relax and a part of the surface deformation becomes irreversible. The surface ridge at the contact line behaves something like a "surface defect" which pins the contact line. The contact line has to jump over this defect for advancing, resulting in the stick-slip motion.

● Regime (iii): in the other extreme situation, when the contact line advances slowly and f is sufficiently low ($f \ll f_{cross}$), the deformation of the gel surface totally relaxes until the contact line moves over a distance of the order R. In this case, the gel substrate behaves nearly like a sheet of very viscous liquid with respect to the contact line motion. As the contact line moves, a capillary flow is driven below the gel surface due to the position shift of the surface force. The surface deformation is transported forward by this capillary flow, following the motion of the contact line. Therefore, the contact line exhibits a continuous advancing motion. This is also consistent with the formation of the lens-like dimple shown in Fig. 4(c″). (Note: at an early stage in Fig. 4(c), there are two stick-slip motions. However, as the total inflation time (≈ 6000 s) is sufficiently long, the surface ridges formed at these two stick points already relax.) Now looking back at the regime (ii) in comparison with the regime (iii), the onset of the stick-slip motion f_{c2} can be interpreted as the frequency at which the flow inside the gel cannot follow the contact line as the elastic stress oppose the substrate flow.
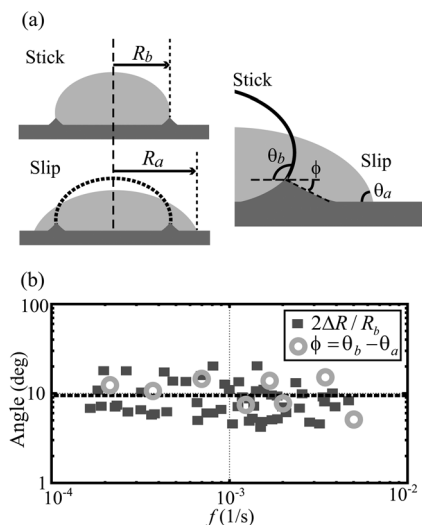
Fig. 9 (a) Parameters for the geometric considerations in the stick-slip regime. R_b, θ_b and R_a, θ_a are radii and contact angles before and after one slip motion, and ϕ indicates the local slope of the surface ridge. (b) Plot of the angle of the local slope of the gel surface predicted from the ratio of successive droplet radii $2\Delta R/R_b$ against f. For comparison, the value of $\phi = \theta_b - \theta_a$ directly obtained from the contact angle measurement is plotted as hollow circles.

The aforementioned mechanism predicts that the rheological property of the gel, especially the crossover frequency f_{cross}, largely affects the transition of the contact line motions (i)–(iii). This is also consistent with our experimental results. As we have observed in Fig. 7(b), both the critical frequencies f_{c1} and f_{c2} drastically change depending on the f_{cross}. The contact line mostly exhibits the regime (i) on a rigid gel of low f_{cross}, while on a soft gel of high f_{cross}, the regimes (ii) and (iii) become more prominent.

C Simple geometric considerations in the stick-slip regime

In this section, we propose geometric considerations in the stick-slip regime (ii) that allow prediction of the link between jumps of the radius and jumps of the apparent contact angle. The schematic of our model is depicted in Fig. 9(a). Inspired by the model of contact angle hysteresis on an elastomer by Extrand and Kumagai,[34] here we consider a simple geometric relation of droplet shapes just before and after one slip motion. The variables R_b, θ_b and R_a, θ_a are the droplet radii and apparent contact angles before and after the contact line slips on the surface ridge, and ϕ indicates the angle of the local slope of the surface ridge.

Considering that the droplet volume V is conserved between before and after the slip, the relations of droplet radii and contact angles are expressed as

$$V = \frac{\pi R_b^{\,3}}{3}(2 - 3\cos\theta_b) = \frac{\pi R_a^{\,3}}{3}(2 - 3\cos\theta_a). \quad (6)$$

We suppose that θ_a is an advancing contact angle on an undeformed surface, and that the difference between θ_b and θ_a is essentially due to the local surface slope. To advance on an inclined surface, the contact line has to take an advancing angle equal to

$$\theta_b = \phi + \theta_a. \quad (7)$$

As θ_a is close to 90° in our case, eqn (6) and (7) are re-written as a function of the ratio of two radii

$$\left(\frac{R_a}{R_b}\right)^3 = \frac{2 - 3\cos(\theta_a + \phi)}{2 - 3\cos\theta_a}, \quad (8)$$

$$\approx 1 + \frac{3}{2}[\cos\theta_a - \cos(\theta_a + \phi)]. \quad (9)$$

With an approximation that ϕ is sufficiently small, the ratio R_a/R_b relates to ϕ as shown in the following expression

$$\frac{R_a}{R_b} \approx 1 + \frac{1}{2}[\cos\theta_a - \cos(\theta_a + \phi)], \quad (10)$$

$$\approx 1 + \frac{\phi}{2}. \quad (11)$$

This equation links the ratio of successive droplet radii to the local surface slope ϕ

$$\phi = \frac{2(R_a - R_b)}{R_b} = 2\frac{\Delta R}{R_b}. \quad (12)$$

In order to check this model, we used the experimental data of $c_{SBS} = 10\%$ in the stick-slip regime (ii) and calculated the quantity $2\Delta R/R_b$ for various stick-slip motions. We compared it to the value of $\phi = \theta_b - \theta_a$ extracted from the direct measurement of the contact angle θ. Fig. 9(b) shows the plot of $2\Delta R/R_b$ and ϕ as a function of the characteristic frequency f. Both quantities are noted nearly equal, which indicates that our model has captured successfully the essential features.

Alternatively, the local slope of the gel surface close to the contact line was measured from the profile curve in Fig. 6(a). The experimental data give the slope angle *ca.* 6.5° at $x = 10$ μm, which is close to the value 10° obtained here.

Finally, let us close this section by qualitatively discussing the fact that ϕ remains locked at the value 10° independently of f. These results are a bit surprising because in available modeling in eqn (1),[24,25] the local slope of the surface ridge $h'(x)$ depends on the elastic modulus G and thus, here, indirectly on f, and even diverges near $x = 0$.

All seems here to happen as if ϕ is selected by some truncation of this profile at a small scale eliminating the contribution of G. In recent studies of wetting on an elastomer, this truncation of the surface profile at the contact line was proposed to be ruled by the surface tension of the substrate γ_s,[27–29] as observed experimentally by Jerison *et al.*[27] In short, for a scale smaller than the elasto-capillary length $l_e = \gamma_s/G$, which plays a role of cut-off, the surface profile is locally determined by the balance of three interfacial tensions and does not depend on the substrate elasticity. For a paraffin gel, the typical value of γ_s is 30 mN m^{-1},[35,36] giving the value of $l_e \approx 6$ μm for $G = 5$ kPa. This value is smaller than our experimental resolution, but it has the right order of magnitude. In addition to this putative cut-off length, when we look at Fig. 6(b), the profile of the surface in the vicinity of the contact line (10 μm ≤ x ≤ 50 μm) does not evolve significantly within

our time window. From these remarks, it is quite natural that ϕ does not depend on f.

Although the models for the wetting on an elastomer cannot be applied directly here as the paraffin gel is visco-elastic and the three interfacial tensions cannot be balanced in our case ($\gamma > 2\gamma_s$), our results suggest that one of their main prediction, *i.e.* the relevance of the elasto-capillary length at a small scale, could also hold in this very complex problem. Further studies will be expected to conclude this proposition definitely.

V Conclusion

In this paper, we have studied the dynamics of water sessile droplets advancing on visco-elastic SBS–paraffin gel substrates. We have observed that the droplet contact line exhibits three different regimes of motions, and their transition is characterized by a frequency of the surface deformation f determined by the apparent contact line velocity v and droplet radius R as $f = v/R$. At high f with respect to the cross-over frequency of gel f_{cross}, the contact line moves continuously with a constant contact angle. As the contact line slows down and f approaches to f_{cross}, the contact line starts the stick-slip motion: the contact line is pinned at a certain position and then suddenly slips forward. In this stick-slip regime, the contact line leaves circular stripe ridges on the gel surface. At f sufficiently lower than f_{cross}, the contact line stops the stick-slip motion and advances continuously again.

We have conjectured that the observed transitions of the contact line motions (continuous–stick-slip–continuous) are the consequence of the rheological property of the gel affecting the dynamics of the contact line. Depending on the frequency, the behavior of the liquid contact line on gels shows both aspects of wetting on elastic solids and on viscous liquid sheets. At an intermediate frequency where the gel behaves neither as a solid nor as a liquid, the stick-slip motion appears. Simple geometrical considerations in the stick-slip regime have also been proposed.

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